

Quantum Storage of Heralded Single Photons in a Praseodymium Doped Crystal

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We report on experiments demonstrating the reversible mapping of heralded single photons to long lived collective optical atomic excitations stored in a $\text{Pr}^{3+}:\text{Y}_2\text{SiO}_5$ crystal. A cavity-enhanced spontaneous down-conversion source is employed to produce widely non-degenerate narrow-band (≈ 2 MHz) photon-pairs. The idler photons, whose frequency is compatible with telecommunication optical fibers, are used to herald the creation of the signal photons, compatible with the Pr^{3+} transition. The signal photons are stored and retrieved using the atomic frequency comb protocol. We demonstrate storage times up to $4.5 \mu\text{s}$ while preserving non-classical correlations between the heralding and the retrieved photon. This is more than 20 times longer than in previous realizations in solid state devices, and implemented in a system ideally suited for the extension to spin-wave storage.

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Many protocols in quantum information science rely on the efficient and reversible interaction between photons and matter [1]. The interaction lays the basis for the realization of quantum memories for light and of their application, e.g. in quantum repeaters [2, 3]. Possible choices for the system used to store light are single atoms in cavities [4], cold or hot atomic gases [5–14], or rare earth (RE) doped solid state systems [15]. Thanks to the weak interaction between the optical active ion and the environment, the RE doped crystalline insulators offer, when cryogenically cooled, the long optical and spin coherence times typical of atomic systems, free of the drawbacks deriving from atomic motion [16]. Moreover they possess the benefits of the solid state systems, such as strong interaction with light, allowing for efficient storage of photons [17, 18] and prospect for integrated devices. Furthermore, their inhomogeneously broadened absorption lines can be tailored in appropriate structures, like atomic frequency combs (AFCs), to enable storage protocols with remarkable properties (e.g. temporal or frequency multiplexing) [19–25].

Storage of qubits encoded in weak coherent states at the single photon level was observed with AFC storage in the excited state [19, 26–29] and, more recently, extended to the ground state in the regime of a few photons per pulse [30]. The storage of non-classical light generated by spontaneous parametric down-conversion (SPDC) has been demonstrated and enabled entanglement between one photon and one collective atomic excitation in a crystal [31, 32], entanglement between two crystals [33], and single photon qubit storage [34, 35]. However, the mapping of non-classical light was obtained so far only in the excited state and furthermore in two-level systems, thus not directly extendable to spin-wave storage.

On the contrary, Pr^{3+} or Eu^{3+} doped crystals have the required level structure for spin-wave storage [23, 24, 30].

In particular, Pr^{3+} doped into Y_2SiO_5 has been exploited to realize devices for the storage of weak coherent states with the highest storage efficiency among the solid state systems (69%) [17]. Moreover, classical images were stored for times of the order of 1 minute [36], i.e. the longest so far obtained among all the investigated systems. Despite these extraordinary performances, which make $\text{Pr}^{3+}:\text{Y}_2\text{SiO}_5$ an excellent candidate for quantum memories, the storage of quantum light has never been achieved in this material. As a matter of fact, the pseudoquadrupolar interaction which splits the crystal-field singlets into hyperfine sub-levels, providing the three-fold ground state required for the storage in the spin state, also establishes a tight bound (< 4 MHz) to the bandwidth of the single photons to be stored. Recently a SPDC source has been developed to create ultranarrowband photon-pairs, with the signal and the idler photons compatible with the Pr^{3+} transition at 606 nm and with telecommunication optical fibers, respectively [37].

In this Letter we report on experiments where one photon of the pair (signal), whose presence is heralded by the other photon (idler), is stored as a collective optical atomic excitation in a $\text{Pr}^{3+}:\text{Y}_2\text{SiO}_5$ crystal with the AFC protocol. We show that the non-classical correlation between the two photons is preserved for storage times up to $4.5 \mu\text{s}$, more than 20 times longer than what was observed in previous solid state experiments [31, 32].

The AFC scheme [20] relies on the creation of a series of narrow absorbing peaks with periodicity Δ in the inhomogeneous absorption profile of the crystal. The single photon is then mapped onto the crystal, leading, in the ideal case, to a single collective optical excitation [31, 32]. After an initial inhomogeneous dephasing, the atoms will rephase after a time $\tau = 1/\Delta$ giving rise to a re-emission of the photon in the forward direction, the so called AFC echo [19]. Figure 1(a) represents the experimental setup.

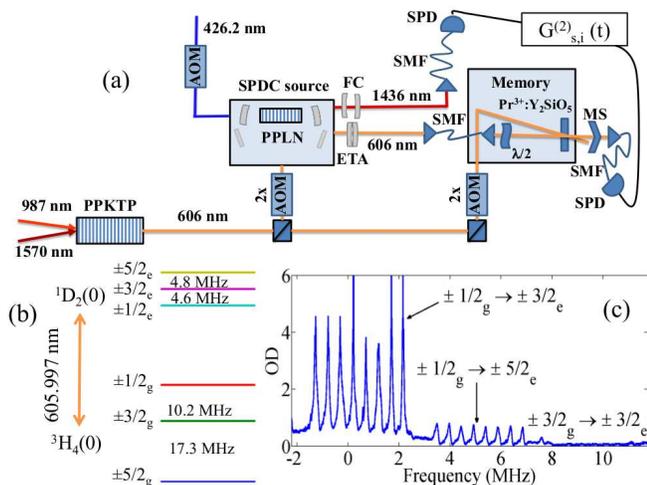


FIG. 1: (Color online) (a) Experimental setup. AOM, acousto-optic modulator (2x when double pass); FC, filter cavity; ETA, etalon; SMF, single-mode fiber; MS, mechanical shutter; SPD, single photon detector; $\lambda/2$, half-wave plate; (b) Energy level scheme of Pr^{3+} in Y_2SiO_5 restricted to the fundamental levels of the ground $^3\text{H}_4$ and the excited $^1\text{D}_2$ manifolds. (c) Example of AFC with $\Delta = 500$ kHz.

The coherent light at 606 nm is obtained using a periodically poled KTiOPO_4 (PPKTP) waveguide (AdVR, Inc.) by means of sum frequency generation (SFG) of 1570 nm and 987 nm light. The sources for these are amplified diode lasers (Toptica, DL 100 pro and TA PRO, respectively) [23]. The frequency of the 606 nm light is locked with the Pound-Drever-Hall technique to a temperature stabilized cavity assembled in a home-made vacuum chamber (2×10^{-7} mbar). The cavity has a finesse $\mathcal{F} \approx 787$ and a free spectral range (FSR) of 1 GHz, leading to a bandwidth of 1.27 MHz. Two beams are spatially separated, the first being used as a frequency reference for the photon-pair source [37] and the second for the memory preparation [23]. Their frequency and amplitude are varied by double-pass acousto-optic modulators (AOMs) driven by an arbitrary waveform generator (Signadyne). After the AOMs, the beams are coupled into polarization maintaining single-mode fibers (SMFs) and out-coupled in two separated optical benches hosting the source and the cryostat (closed cycle cryogenic cooler, Oxford V14), which is exploited to cool the $\text{Pr}^{3+}:\text{Y}_2\text{SiO}_5$ crystal down to 2.8 K.

The heralded single photons are obtained from the photon-pair source, whose detailed description is given in ref. [37]. A CW pump beam at 426.2 nm (Toptica, TA SHG), modulated by an AOM, produces photons at 606 nm (signal) and 1436 nm (idler) by SPDC in a temperature-stabilized PP lithium niobate (LN) crystal. A bow-tie cavity surrounding the crystal enhances the SPDC process for the resonant frequencies. The cavity is stabilized with the reference beam at 606 nm, to ensure

the signal resonance with the $\text{Pr}^{3+}:\text{Y}_2\text{SiO}_5$ crystal. At the same time, to maintain the cavity resonant with the idler, the pump frequency is locked using light at the idler frequency created by difference frequency generation of the pump and the 606 nm reference beam. The double resonance allows a very efficient suppression of the redundant spectral modes due to the so called clustering effect [37]. The photon-pairs' spectrum is composed of a main- and two secondary-clusters separated by 44.5 GHz, each containing four longitudinal modes [37]. In order to operate in the single-mode regime, the heralding telecom photons are filtered by a home-made filter cavity (FC, linewidth ≈ 80 MHz and FSR ≈ 16.8 GHz, mirrors from Layertec GmbH). An etalon (linewidth ≈ 6 GHz and FSR ≈ 60 GHz, LightMachinery) is placed in the signal arm as well, resulting in the mere suppression of the secondary-clusters. Further suppression of the unwanted spectral modes within the main-cluster is provided in the 606 nm arm by the inhomogeneously broadened absorption profile of Pr^{3+} . The correlation time of the photon-pair is measured from the signal-idler cross-correlation function $G_{s,i}^{(2)}(t)$ to be $\tau_c = 108$ ns, corresponding to a photon bandwidth of $\delta\nu = 2.3$ MHz (1.84 MHz) for the signal (idler) photons [37]. In order to protect the single photon detectors (SPDs) from the reference beams and to avoid excess noise, the lock and the measurement times are alternated (with 45 % duty cycle) by mechanical choppers. The telecom photons are detected immediately after the FC by a InGaAs SPD (IdQuantique id220, detection efficiency $\eta_{d,i} = 10\%$ and 400 Hz dark count rate) and are used to herald the creation of the 606 nm photons, which are sent to the memory via a SMF. The optical transmission of the signal (idler) photon from the output of the bow-tie cavity to the cryostat (SPD) is $\eta_s = 0.18$ ($\eta_i = 0.18$). To optimize the detection of the stored and retrieved photons, we switch off the pump beam using the AOM after the detection of an idler photon (500 ns before signal photon is re-emitted by the crystal), thus interrupting the creation of new photon-pairs.

Our storage device is a 3 mm thick Y_2SiO_5 sample doped with a Pr^{3+} concentration of 0.05 %. The relevant optical transition is at 605.977 nm with a measured absorption coefficient of $\alpha = 23 \text{ cm}^{-1}$ and an inhomogeneous linewidth of 5 GHz [23]. A half-wave plate ($\lambda/2$) ensures the polarization of the photons to be aligned close to the optical D_2 axis of the crystal, in order to maximize the absorption [38]. To prevent noise from the strong preparation beam polluting the single photon mode, we use two different optical paths with an angle of 2.5 degrees. The maximum power in the preparation mode before the cryostat window is 6 mW and the beam diameter at the crystal is $150 \mu\text{m}$. The beam diameter for the input mode is $50 \mu\text{m}$. The single photon mode is directed to a Si-SPD (Excelitas Technologies, efficiency $\eta_{d,s} = 40\%$ and 10 Hz dark counts) via a SMF with 60 % coupling efficiency. A mechanical shutter is employed to

protect the SPD during the preparation of the spectral features (300 ms long); the duty cycle is 50 %.

To prepare the memory we follow the procedure thoroughly described in [23, 39]. We prepare a transparency window within the inhomogeneously broadened Pr^{3+} absorption at 606 nm by sweeping the laser frequency by 12 MHz. The comparatively narrow transparency window contributes to select only one mode among the four remaining in the main-cluster of the source spectrum and are separated by 412 MHz [37]. Afterwards we tailor a single class AFC on the $\pm 1/2g - \pm 3/2e$ transition by first burning back atoms with pulses at frequencies differing by Δ and then performing a cleaning sweep in the region of the $\pm 3/2g - \pm 3/2e$ transition (see Fig. 1(b)). To ensure the efficient absorption of the photons by the periodic structure, the total comb-width is set to 3.5 MHz (see Fig. 1(c) for an example with $\Delta = 500$ kHz). With the present preparation procedure we are able to tailor spectral features as narrow as 60 kHz. The input photon frequency is selected to be resonant with the $\pm 1/2g - \pm 3/2e$ transition.

The arrival times of the photons to the detector are recorded with a time-stamping card (Signadyne) and used to reconstruct the second-order cross-correlation function between signal and idler $G_{s,i}^{(2)}(t)$. A figure of merit for the non-classical nature of the photon correlations is the normalized cross-correlation function [3, 31]

$$g_{s,i}^{(2)} = \frac{p_{s,i}}{p_s p_i}, \quad (1)$$

where p_s (p_i) is the probability to detect a signal (idler) photon and $p_{s,i}$ the probability to detect a coincidence in a time window $\Delta t_d = 400$ ns centered at zero time delay. All the results presented in this paper are from raw data, without any background or dark count subtraction.

We first characterize the input heralded single photon by sending it through the memory crystal when only a transparency window is created (see blue histogram centered at zero time delay in Fig. 2(a)). The values of $g_{s,i}^{(2)}$ as a function of the pump power P_p are plotted in Fig. 2(b). Despite the expected decrease for increased pump powers [40], the values remain well above the classical limit of 2 (dotted line) for two-mode squeezed states.

In order to unambiguously confirm the non-classical nature of the correlation, we also measure the marginal auto-correlation function for the signal and idler mode, $g_{s,s}^{(2)}$ and $g_{i,i}^{(2)}$ (see Supplemental Material). We find, at pump power of 5 mW, $g_{s,s}^{(2)} = 1.14 \pm 0.03$ and $g_{i,i}^{(2)} = 1.07 \pm 0.02$, leading to strong violation of the Cauchy-Schwarz inequality in the form $R = (g_{s,i}^{(2)})^2 / (g_{i,i}^{(2)} \times g_{s,s}^{(2)}) = 61 \pm 3 \not\leq 1$.

The detected coincidence rate (within Δt_d) is $C_d = (0.83 \pm 0.14)$ Hz/mW. From this value, we infer the generated coincidence rate C_g at the output of the cavity $C_g = C_d / (\eta_i \cdot \eta_{d,i} \cdot \eta_s \cdot \eta_{loss} \cdot \eta_{d,s}) = 3.4$ kHz/mW, where

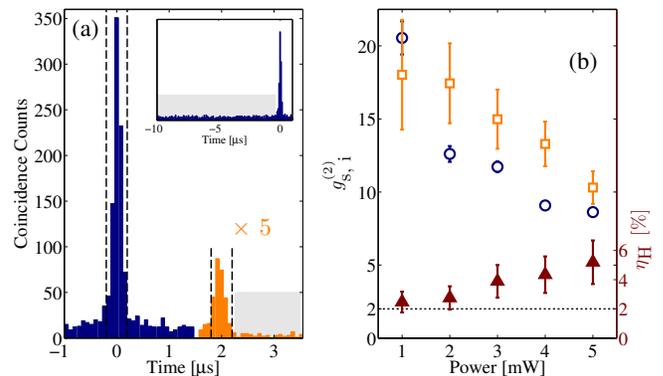


FIG. 2: (Color online) (a) $G_{s,i}^{(2)}(t)$ histogram without (blue) and with (orange) AFC. The preprogrammed storage time is $2 \mu\text{s}$ and the power of the 426.2 nm pump is 2 mW. The time-bin size is 5 ns. The dashed lines and shaded area define the detection windows for the coincidences ($\Delta t_d = 400$ ns) and noise, respectively, used to compute $g_{s,i}^{(2)}$. (b) The $g_{s,i}^{(2)}$ values as a function of the pump power for the AFC echo (empty squares) are compared to those for the input photons (empty circles). The heralding efficiencies η_H are also reported (filled triangles). The integration times range between 30 and 60 minutes. The error bars are evaluated from the raw number of counts assuming Poissonian statistics. The dotted line corresponds to the classical limit $g_{s,i}^{(2)} = 2$ for two-mode squeezed states.

$\eta_{loss} = 0.225$ is the transmission from the input of the cryostat to the signal SPD, including the duty cycle of the memory. We can also evaluate the heralding efficiency in front of the cryostat, $\eta_H = p_{s,i} / (p_i \times \eta_{d,s} \times \eta_{loss})$, whose values as a function of P_p are reported in Fig. 2(b) (full triangles). η_H is mainly limited by η_s and dark counts in the heralding SPD. Subtracting the contribution of the 1436 nm detector dark counts we find heralding efficiencies almost constant, $\eta_H^{DC} \approx 6.3\%$, over the whole range of pump powers investigated. Finally, we estimate that more than 95 % of the heralded signal photons detected after the crystal are resonant with the atoms (see Supplemental Material) [41].

Once the non-classical nature of the input photons propagating through the transparency window is demonstrated, we prepare the AFC and reconstruct the $G_{s,i}^{(2)}(t)$ function for the stored and retrieved photons. Figure 2(a) includes the coincidence histogram when an AFC is producing a collective re-emission at a delay of $\tau = 2 \mu\text{s}$ (orange trace). The values of $g_{s,i}^{(2)}$ for the AFC echo as a function of the P_p are reported in Fig. 2(b) (empty squares). The count rate in the region of the AFC echo is $C = (0.043 \pm 0.03)$ Hz/mW. We observe that the echoes exhibit $g_{s,i}^{(2)}$ values higher than the input photons. We attribute this unexpected effect to the fact that the AFC acts as a temporal filter [42] for non-resonant noise arising from the SPDC source. Since the SPDC pump laser is turned off after the detection of an idler photon, the AFC

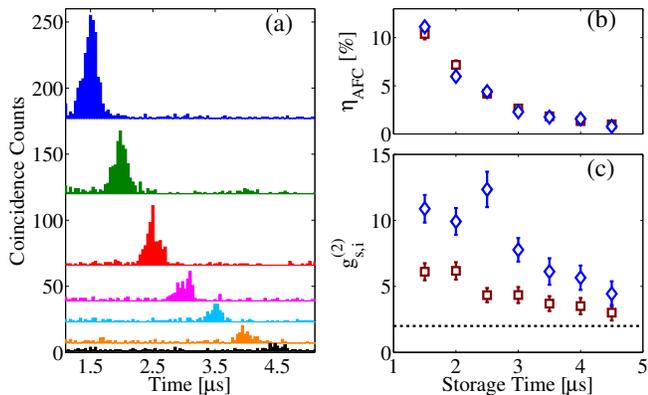


FIG. 3: (Color online) (a) AFC echoes at different predetermined storage times observed in coincidence histograms measured at 2 mW pump power (integration time is 40 minutes and the time-bin size is 5 ns). The curves are vertically shifted for clarity. (b) and (c) AFC efficiency and $g_{s,i}^{(2)}$ (calculated in a 400 ns window) of the AFC echo as a function of the storage time. Diamonds: filter cavity in the heralding photon path; squares: filter cavity removed from the heralding photon path. The error bars are evaluated from the raw counts assuming Poissonian statistics. The dotted line corresponds to the classical limit $g_{s,i}^{(2)} = 2$ for two-mode squeezed states.

delays the signal to a region free of broadband noise, thus increasing the $g_{s,i}^{(2)}$. A more quantitative analysis of this effect is presented in the Supplemental Material. When the pump power decreases, the detection of the echo is limited by the detector dark counts. This gives rise to a saturation of the echo $g_{s,i}^{(2)}$ values which hides the filtering effect of the storage.

In view of applications in temporally multi-mode quantum memories with on-demand read-out, the pre-programmed delay τ must be tunable to allow the application of control pulses transferring the excitation to the spin states [23]. Thus, we changed the spectral periodicity Δ of the AFC to obtain increased delays. Figure 6(a) shows the coincidence histograms in the region of the AFC echo occurring at different predetermined storage times. The AFC storage efficiency, η_{AFC} , is estimated by comparing the number of counts of the input propagating through the transparency window and the echo; it decreases for longer delays, as shown in Fig. 6(b), denoting a reduction of the comb finesse [19]. We note that the AFC efficiency with single photons does not decrease with respect to the storage of bright pulses or weak coherent states at the single photon level (the different cases together with a theoretical evaluation are compared in the Supplemental Material). This confirms that there is no significant frequency jitter for the single photons. Compared to previous experiments of single photon storage in solid state devices based on other materials [31, 32], we could reach AFC storage times more than 20 times longer, while preserving non-classical cor-

relations (see Fig. 6(c)). As we stop the production of pairs after the detection of a telecom photon, the region where the echo lies should not be affected by unconditional noise coming from the source (see Supplemental Material). Thus, despite the reduction in the AFC efficiency, the echo should exhibit constant values of $g_{s,i}^{(2)}$ for increasing storage times. As a matter of fact, the decrease in the $g_{s,i}^{(2)}$ values while increasing the storage time is less pronounced than the drop of the AFC efficiency (compare the diamonds in panels (b) and (c) of Fig. 6) and we attribute the reduction to the limitation given by the detector dark counts.

We also report the values of η_{AFC} and $g_{s,i}^{(2)}$ measured without the FC in the idler arm. The efficiencies in the two cases agree within the experimental error. On the contrary, despite the factor 2 gain in the raw number of counts thanks to the reduced passive losses, the $g_{s,i}^{(2)}$ without FC decreases due to the frequency multimodality of the source [37]. In fact, among the four modes coexisting in the main-cluster, only one is resonant with the AFC. The non-resonant modes in the idler arm join the start signals for the coincidence histogram without corresponding stops (the Pr^{3+} absorption acts as a filter for the non-resonant mode in the 606 nm arm), thus decreasing the heralding efficiency and contributing to the noise increase. Note that frequency multiplexed quantum light storage could be obtained by creating several AFCs at different frequencies separated by the SPDC cavity FSR [25].

In conclusion, we have demonstrated the reversible mapping of heralded single photons to collective optical atomic excitations in a praseodymium doped crystal. We observed an increase of non-classical correlations between signal and idler photons during the storage, thanks to a temporal filtering effect due to the AFC. Storage times up to 4.5 μs while preserving quantum correlations were observed, more than 20 times longer than previous solid state experimental realizations. Furthermore, the transition used would readily allow the transfer of the excitation to the ground state to obtain long-lived spin-wave storage of quantum state of light, provided that the noise induced by the control beams can be sufficiently reduced. We note that this is the longest storage reported so far for a single collective optical atomic excitation and that it would enable the entanglement between crystals separated by km range distance.

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Supplemental Material

We report, in the present supplemental material, details about the experimental setup, the characterization of the AFC storage with bright pulses and weak coherent states, the second-order auto-correlation measurements of signal and idler photons, and the second-order cross-correlation measurements between signal and idler as a function of the signal photons polarization.

Setup

In the present section we provide additional details about the setup and the measurements. We start from the passive losses along the signal and idler optical paths with the purpose of estimating the effective performances of the photon-pair source starting from the detected count-rates.

TABLE I: Transmission of the single optical elements, T , and detector efficiencies, η_d , in the signal (606 nm) and idler (1436 nm) arm.

Element	T/η_d (signal)		T/η_d (idler)
Dichroic Mirror	> 99 %		76 %
Glass Plate	84 %		80 %
Band Pass Filter	95 %		
Etalon	90 %	η_s, η_i	
Filter Cavity			50 %
Fiber	31 %		60 %
Other optical elements	80 %		
Cryostat	75 %		
Fiber	60 %	η_{loss}	
Memory duty cycle	50 %		
SPD	32 %		10 %

Table I summarizes the transmission of the single optical elements along the path of the signal and the idler photons at 606 nm and 1436 nm, respectively. The total transmission of the signal (idler) photons from the SPDC cavity to the cryostat (SPD) is $\eta_s = 18\%$ ($\eta_i = 18\%$). Figure 4 shows an illustration of the source and memory duty cycles. The former, 45 %, derives from the alternation of the SPDC cavity lock and the photon-pair production. We note that, during the locking period, the measured count rate is the detector dark count. The memory duty cycle, 50 %, is associated with the closure of the mechanical shutter placed after the $\text{Pr}^{3+}:\text{Y}_2\text{SiO}_5$ crystal and aimed at protecting the 606 nm SPD from the eventual leakage of the strong preparation beam into the echo mode. During the preparation time we also gate the SPD. While the source duty cycle is the same for the signal and idler photons, the memory duty cycle only

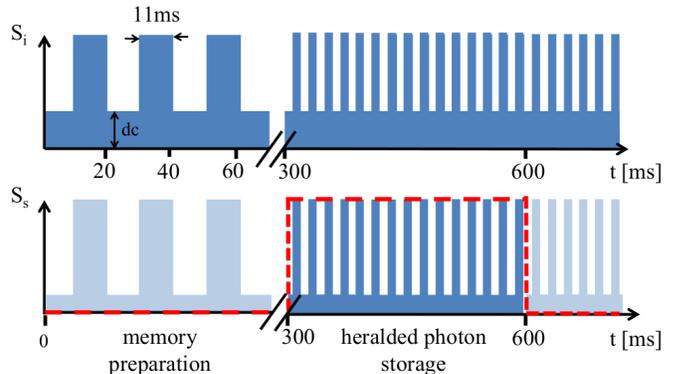


FIG. 4: (Color online) Illustration of the source (blue bars) and memory (dotted line) duty cycles.

affects the signal photons, thus altering the detected coincidence rate, C_d . For this reason, the transmission of the 606 nm photons from the cryostat to the signal detector, $\eta_{loss} = 22.5\%$, also takes into account the memory duty cycle.

During the measurement time, we optimize the detection of the stored and retrieved photons by switching off the pump beam after the detection of an heralding photon. This interrupts the SPDC process and prevents the production of noise due to uncorrelated photons in the region of the coincidence histogram where the AFC echo is expected to occur. Figure 5 shows an illustration of the coincidence histograms for the input (solid curve) and the retrieved (dashed curve) photons, where the noise drop is emphasized by an arrow. The time delay between the idler photon detection and the pump turning off changes with the storage time, being modulated in order the noise drop to occur 500 ns before the absorbed photons are re-emitted. This allows us to measure the noise affecting the echo in an appropriately large window. The pump beam remains off during $20\mu\text{s}$.

Memory characterization

Before the single photon storage experiments, we characterize our memory initially with bright pulses and then with weak coherent states obtained from a laser beam strongly attenuated with a set of neutral density filters. In both cases we use gaussian pulses with a duration comparable with the correlation time of the photon-pairs produced by the SPDC source, i.e. 108 ns. The mean number of photons μ is evaluated from the raw number of counts detected by the SPD when the AFC is not prepared, back-propagated taking into account the detector

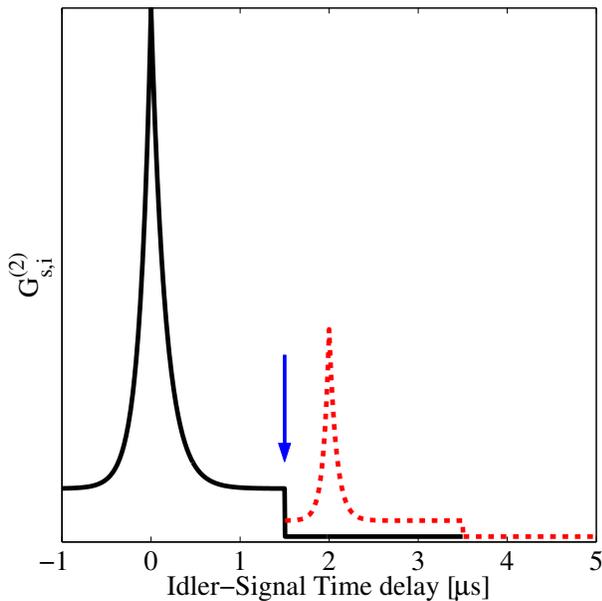


FIG. 5: (Color online) Illustration of the $G_{s,i}^{(2)}(t)$ cross-correlation function for the signal photons when passing through the transparency window (black solid curve) and being absorbed and reemitted by the AFC (red dashed curve). The arrow indicates the noise drop due to the pump beam switching off.

efficiency, the coupling efficiency into the fiber, and the losses induced by the crystal when a transparency window is prepared (see Table I).

Fig. 6 reports the AFC echo efficiency obtained at increasing storage times for bright pulses (squares), weak coherent states (diamonds), and single photons (circles). The mean number of photons in the weak coherent pulses is fixed to $\mu = 0.01$, to be of the same order of magnitude as the heralding efficiency of the SPDC source. We stress that observing a constant AFC echo efficiency when moving from bright pulses, obtained from a stabilized laser beam, to single photons, implies the frequency jitter of the photon-pair source to be limited and the double locking system efficient.

In the framework of the theoretical model presented in ref. [20], the AFC echo efficiency can be expressed as

$$\eta_{AFC} \approx \tilde{d}^2 e^{-7/F^2} e^{-\tilde{d}} e^{-d_0}, \quad (2)$$

where $F = \Delta/\gamma$ is the finesse of the comb with γ being the peak width, $\tilde{d} = d/F$ is the effective optical depth experienced by the absorbed photons with d being the optical depth of the peaks, and d_0 is the absorbing background. From the example of AFC shown in Fig. 1(b) of the main text, we extract the average peak width and separation, optical density and absorbing background ($\gamma = (76 \pm 9)$ kHz, $\Delta = (488 \pm 7)$ kHz, $d = 4.9 \pm 0.4$, and $d_0 = 0.56 \pm 0.03$, respectively) and we predict $\eta_{AFC} = (13 \pm 3)\%$ for a storage time of $2 \mu\text{s}$, to be

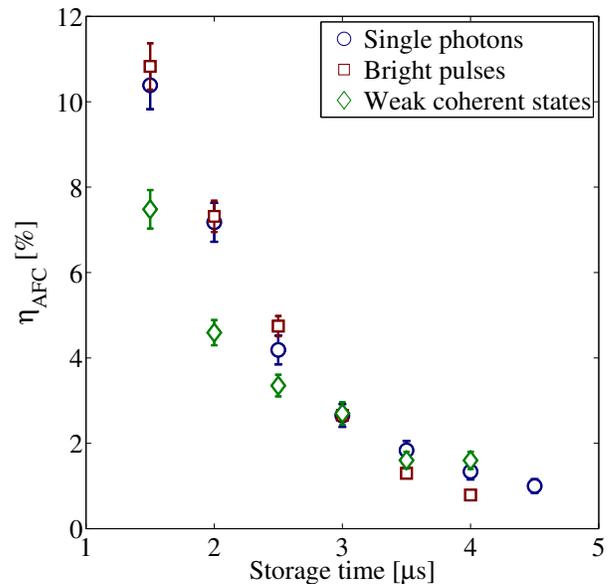


FIG. 6: (Color online) AFC echo efficiency as a function of the storage time for bright pulses (squares), weak coherent states (diamonds) and single photons (circles).

compared with the value of $\eta_{AFC} = (7.2 \pm 0.5)\%$ observed in the heralded single photon storage (see Fig. 6). The disagreement between the expected and the measured efficiency might be due to a not complete absorption of the photons due to the difference between the AFC total width and the photon bandwidth. It is worth noting, however, that the comb optical density might be underestimated due to the limited dynamic range of the detector. This could lead to the overestimation of the peak width and, consequently, of the theoretical AFC efficiency due to a suboptimal finesse. Note also that higher efficiencies could be reached by tailoring square AFC peaks [43].

Second-order auto-correlation measurements

For a pair of independent classical fields, the Cauchy-Schwarz inequality must be fulfilled [44]:

$$R = \frac{(g_{s,i}^{(2)})^2}{g_{i,i}^{(2)} \times g_{s,s}^{(2)}} \leq 1 \quad (3)$$

where $g_{s,s}^{(2)}$ and $g_{i,i}^{(2)}$ are normalized second-order auto-correlation functions for signal and idler fields, respectively. The light emitted by spontaneous down conversion is usually well approximated by two-mode squeezed states, which exhibit thermal statistics for the signal and idler fields, i.e. $g_{s,s}^{(2)}, g_{i,i}^{(2)} = 2$ [45]. Under the assumption of two-mode squeezed states, measuring $g_{s,i}^{(2)} > 2$ is therefore sufficient to violate the Cauchy-Schwarz inequality and give strong evidence of non-classical correla-

tions. However, in order to obtain a violation of Cauchy-Schwarz inequality without assumptions on the created state, it is required to measure directly $g_{s,s}^{(2)}$ and $g_{i,i}^{(2)}$. We thus assembled a Hanbury Brown-Twiss set-up, inserting fiber beam-splitters after the cryostat in the 606 nm arm (Thorlabs), when only a transparency window is created, and after the filter cavity in the 1436 nm arm (AFW Technologies). Additional SPDs are employed after the fiber beam-splitters for the detection of the 606 nm and the 1436 nm photons (Count from Laser Components and id210 from ID Quantique, respectively).

Figure 7 shows the intensity auto-correlation function of the signal photons at 606 nm measured with a pump power of 5 mW: it exhibits the clear fingerprint of bunching behavior in the fact that the peak maximum at zero delay exceeds unity by several standard deviations. The normalized second-order auto-correlation measured in a time window $\Delta t_d = 400$ ns is $g_{s,s}^{(2)}(\Delta t_d) = 1.14 \pm 0.02$. Figure 7 also reports the fit of the curve according to a symmetric exponential decay about zero delay, from which we extrapolate the decay time $t_c = 265$ ns and the FWHM correlation time $\tau_c = 160$ ns. Analogously, we find for the idler photons a value of $g_{i,i}^{(2)}(\Delta t_d) = 1.07 \pm 0.01$. The non-classical nature of the photon correlation is therefore confirmed, at pump power of 5 mW, by the violation of the Cauchy-Schwarz inequality in the form $R = 61 \pm 2 \not\leq 1$. We also measure $g_{s,s}^{(2)}(\Delta t_d)$ and $g_{i,i}^{(2)}(\Delta t_d)$ at a lower pump power, i.e. 2 mW, leading to higher violation of the Cauchy-Schwarz inequality $R = 142 \pm 10$ (see Table II).

The measured values of $g_{s,s}^{(2)}$ and $g_{i,i}^{(2)}$ are significantly lower than the value of 2 expected for the thermal states produced by SPDC phenomena [45]. We describe here some additional measurements which, joined to a simple model for the noise characterization, provide an explanation of the disagreement between the experimental and the expected values.

Exploiting the same Hanbury Brown-Twiss set-up, we perform auto-correlation measurements of the signal photons when travelling through the $\text{Pr}^{3+}:\text{Y}_2\text{SiO}_5$ crystal without any spectral feature tailored. The inhomogeneously broadened Pr^{3+} profile should act as a filter for the single photons, thus returning a flat coincidence histogram between the two arms of the fiber beam-splitter. However, it gives the measure of any kind of non-resonant, allegedly broadband, noise affecting the system [41].

The red squares in Fig. 8 display the measured second-order auto-correlation function of the photons transmitted by the crystal. We note that no evidence of photon bunching is present, thus ruling out any contribution from the secondary-clusters. In fact, they are separated from the main-cluster by a value (44.5 GHz [37]) significantly higher than the inhomogeneous broadening of the Pr^{3+} optical transition at 606 nm (5 GHz [23]). If they were not completely suppressed by the etalon in the sig-

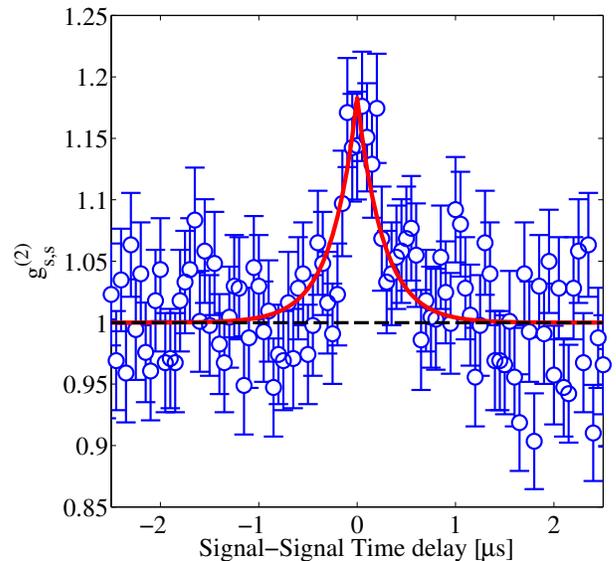


FIG. 7: (Color online) Normalized second-order auto-correlation function of the signal photons. The pump power is 5 mW and the integration time is 18 hours. The time-bin size is 50 ns. The error bars are calculated according to Poissonian statistics.

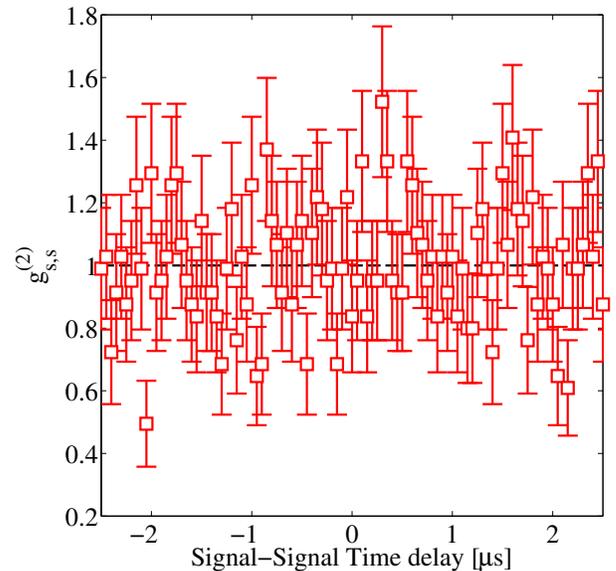


FIG. 8: (Color online) Second-order auto-correlation function of signal photons transmitted by the inhomogeneously broadened line of Pr^{3+} at 606 nm. The pump power is 5 mW and the integration time is 2 hours. The time-bin size is 50 ns. The error bars are calculated according to Poissonian statistics.

nal arm, they would not be absorbed by the crystal and would reach the detector giving a bunching peak.

A quantitative comparison between the two measurements reported in Fig. 7 and Fig. 8 can provide hints about the noise contribution and thus help us to interpret the experimentally obtained $g_{s,s}^{(2)}(\Delta t_d)$ value.

We define $N_A = S_A + B_A$ as the count-rate at the detector A when the transparency window is created. S_A is the SPDC contribution and B_A the background, inclusive of uncorrelated noise and detector dark counts. With the assumption that it is mainly non-resonant with the Pr^{3+} absorption, we extract the background from the count-rate at the same detector in the measurement where no transparency pit is tailored. Analogously, $N_B = S_B + B_B$ is the count-rate at the detector B.

At a time delay much greater than the correlation time, the number of coincidence counts is proportional to the product

$$N_A N_B = S_A S_B + S_A B_B + S_B B_A + B_A B_B, \quad (4)$$

while at zero delay it is proportional to $N_A N_B + S_A S_B$ due to the bunching behaviour of the SPDC photons (assuming thermal statistics). The proportion in both cases is given by the product of the window size and the integration time. The expected value of the intensity auto-correlation function is thus

$$g_{s,s}^{(2)\text{th}}(0) = \frac{N_A N_B + S_A S_B}{N_A N_B} = 1 + \frac{S_A S_B}{N_A N_B}. \quad (5)$$

For $P_p = 5$ mW pump power, we measure background to signal ratios $B_A/S_A = 0.85$ and $B_B/S_B = 0.98$. This leads to value of $g_{s,s}^{(2)\text{th}}(0) = 1.27$. This result suggests that the noise affecting our system is prevalingly non-resonant with the Pr^{3+} absorption.

The inferred $g_{s,s}^{(2)\text{th}}(0)$ refers to the ideal case of an infinitely small integration window about zero delay, thus it is not directly comparable to the experimental value $g_{s,s}^{(2)}(\Delta t_d) = 1.14 \pm 0.02$, which is measured in a finite time window $\Delta t_d = 400$ ns. To take this effect into account, we consider a symmetric exponential decay with decay time t_c for the correlation function and find

$$g_{s,s}^{(2)\text{th}}(\Delta t_d) = g_{s,s}^{(2)\text{th}}(0) \frac{2t_c}{\Delta t_d} (1 - e^{-\frac{\Delta t_d}{2t_c}}) + 1, \quad (6)$$

where the factor of two takes into account the symmetric exponential. For the fitted $t_c = 265$ ns, we find $g_{s,s}^{(2)\text{th}}(\Delta t_d) = 1.19$.

We also perform a similar analysis for a pump power of 2 mW. Table II summarizes the experimental and theoretical values for the different powers of the 426.2 nm pump.

The interpretation of the $g_{i,i}^{(2)}$ value measured for the idler photons deserves a separated discussion. In fact, in this case the background contribution cannot be directly measured as for the signal photons. We note, however, that, due to the presence of the filter cavity in the idler mode and to much higher dark count rates for the SPDs, the background for the infrared photons is dominated by the dark counts of the detectors (400 Hz and

TABLE II: Normalized intensity auto-correlation values of signal and idler photons as obtained from the experimental histogram and from the theoretical model for different powers of the 426.2 nm pump. The R values, as calculated from the experimental values of $g_{s,s}^{(2)}$, $g_{i,i}^{(2)}$, and $g_{s,i}^{(2)}$, are also reported. All values are for a detection window $\Delta t_d = 400$ ns

P_p	2 mW	5 mW
$g_{s,s}^{(2)}$	1.09 ± 0.04	1.14 ± 0.02
$g_{s,s}^{(2)\text{th}}$	1.15	1.19
$g_{i,i}^{(2)}$	1.03 ± 0.01	1.07 ± 0.01
$g_{i,i}^{(2)\text{th}}$	1.003	1.03
$g_{s,i}^{(2)}$	12.6 ± 0.5	8.7 ± 0.2
R	142 ± 10	61 ± 2

1200 Hz for the id220 and id210, respectively). Applying Eq. 5 to the idler photons, where B_A and B_B are evaluated from a dark count measurement, we calculate an expected value of $g_{i,i}^{(2)\text{th}}(\Delta t_d) \approx 1.03$ for 5 mW pump power, in reasonable agreement with the experimental $g_{i,i}^{(2)}(\Delta t_d) = 1.07 \pm 0.01$.

Linear dichroism measurements

To investigate the disagreement between the values for the input and the stored photons of the normalized second-order cross-correlation between signal and idler (see Fig. 2 of the main text), $g_{s,i}^{(2)}$, we perform linear dichroism measurements with the heralded photons transmitted by the inhomogeneous line of the $\text{Pr}^{3+}:\text{Y}_2\text{SiO}_5$ crystal. We collect the $G_{s,i}^{(2)}(t)$ cross-correlation function between signal and idler for different polarizations of the signal photons without preparing either the AFC or the transparency window. From the coincidence histograms we calculate the $g_{s,i}^{(2)}$ values as a function of polarization, considering a time window of 400 ns around the peak at zero delay. An example is given in the inset of Fig. 9 in the case of 3.5 mW pump power.

The main frame of Fig. 9 displays the visibility as a function of the pump power, extracted from the polarization dependence of the coincidences. For pump powers up to 2 mW the conditioned visibility approaches 90 % and it decreases below 70 % when the pump power reaches 3.5 mW. This is a further proof of the existence of a non-resonant noise, whose relative weight with respect of the resonant signal is increasing at higher pump powers. From the measured visibilities we can extract the probability to detect coincidences due to photons not resonant with the Pr^{3+} inhomogeneous absorption line, P_{nr} , with respect of that of detecting coincidences due to resonant ones, P_r .

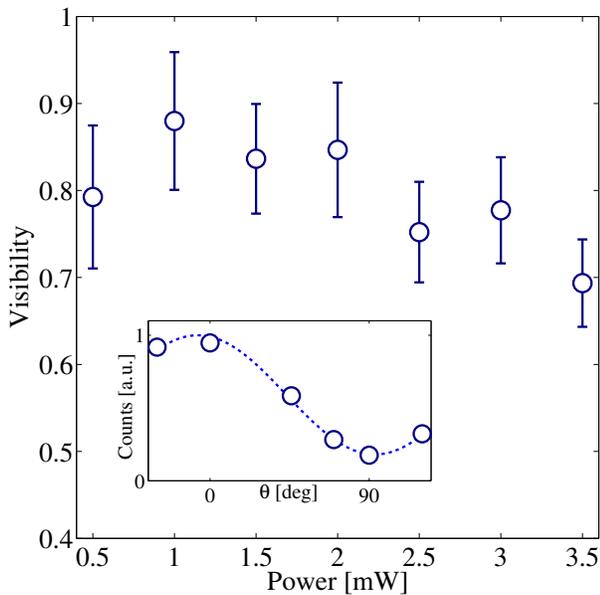


FIG. 9: (Color online) Visibility as a function of the pump power as obtained from coincidence histograms measured with different polarization of the input photons when no transparency window is created. The error bars are calculated according to Poissonian statistics. Inset: Normalized coincidence counts in a 400 ns window as a function of the polarization of the 606 nm photons travelling through the crystal. The pump power is 3.5 mW.

With θ the angle between the light polarization and the optical D_1 axis of the Y_2SiO_5 crystal, we assume that the probability to detect a coincidence behaves as

$$P(\theta) = P_{nr} + P_r \times e^{-OD(\theta)}, \quad (7)$$

where $OD(\theta)$ is the optical density of the Pr^{3+} absorption at that polarization. Taking into account $OD=1.4$ measured in the weakly absorbing polarization (D_1) and $OD=6.9$ for the polarization parallel to the D_2 axis, we evaluate the non-resonant coincidences to be about 1 – 2% of the resonant ones for visibilities varying between 90 and 80%, which is the case for pump powers up to 2 mW. As soon as the visibility drops to values below 70%, the non-resonant to resonant photons ratio exceeds 5%.

The described approach enables quantifying the ratio of signal photons resonant with the Pr^{3+} absorption line with respect of the total photons produced, i.e. 97% for pump powers up to 3 mW and 95% for higher pump powers. We note, however, that a comparison between the coincidence rates measured in a time window $\Delta t_d = 400$ ns for the 606 nm photons passing through the absorption profile and the transparency window (examples at $P_p = 2$ mW are shown in Fig. 10), allows us to conclude that the majority of the photons resonant with the Pr^{3+} inhomogeneous line are also resonant with the transparency window where the AFC is

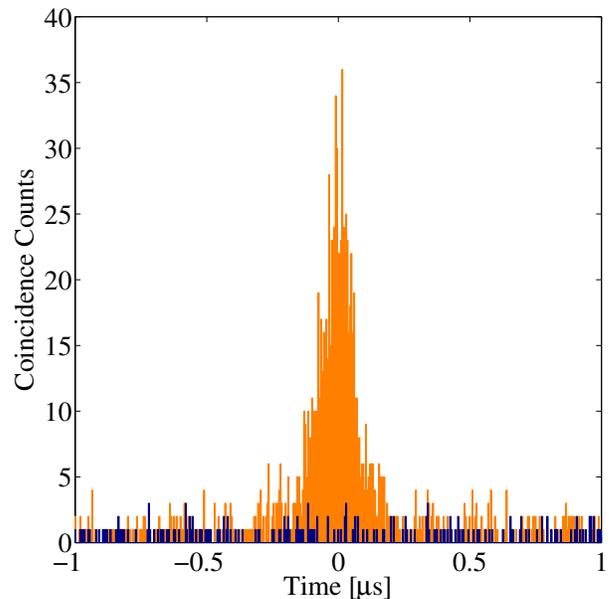


FIG. 10: (Color online) $G_{s,i}^{(2)}(t)$ functions acquired at 2 mW pump power with the signal photons transmitted by the Pr^{3+} inhomogeneous absorption line (blue trace) and travelling through a transparency window (orange trace).

tailored. As a matter of fact, we find for the photons transmitted by the inhomogeneous line of Pr^{3+} a coincidence rate of $C_d = (0.04 \pm 0.1)$ Hz/mW, i.e. less than 5% of the detected coincidence rate of the input photons ($C_d = (0.83 \pm 0.14)$ Hz/mW). In other words, more than 95% of the heralded photons detected after the crystal are resonant with the transparency window.

The non-resonant noise is expected to affect the $g_{s,i}^{(2)}$ values of the input but not those of the stored photons. In fact, the AFC comb selects only a portion of the input photons and returns it in a separated temporal mode, which does not include any uncorrelated noise due to the pump beam switching off after the detection of an idler photon (see Fig. 5).

We now describe a simple picture explaining how, even a small contribution of non-resonant noise, can significantly affect the $g_{s,i}^{(2)}$ values. We can write the normalized intensity cross-correlation in terms of resonant and non-resonant contributions to the coincidence probability as

$$g_{s,i}^{(2)\text{th}} = \frac{p_{s,i}}{p_s p_i} = \frac{P_r + P_{nr}}{P_n + P_{nr}}, \quad (8)$$

where P_n is the probability of having accidental coincidences due to resonant photons. Defining $r = P_{nr}/P_r$, Eq. 8 becomes

$$g_{s,i}^{(2)\text{th}} = \frac{P_r}{P_n} \times \frac{1+r}{1+r(P_r/P_n)}. \quad (9)$$

The ratio P_r/P_n is the normalized second-order cross-correlation after the filtering of any non-resonant contribution. In a picture where the AFC storage returns an echo free of non-resonant photons, it is exactly the $g_{s,i}^{(2)}$ value of the echo. We thus apply the proposed model to predict the $g_{s,i}^{(2)}$ value of the input photons from that of the echo. The measured and predicted values are summarized in Table III for 2 and 3 mW pump power. The prediction of the model is in agreement with the measured values, which confirms that the AFC acts as a temporal filter for non resonant noise [42].

TABLE III: Normalized intensity cross-correlation between signal and idler photons as obtained from the measurements with the signal photons passing through the transparency window, $g_{s,i}^{(2)}$ (input), compared to that estimated, $g_{s,i}^{(2)\text{th}}$, starting from the cross-correlation of the retrieved photons, $g_{s,i}^{(2)}$ (echo), for different powers of the 426.2 nm pump.

P_p	2 mW	3 mW
$g_{s,i}^{(2)}$ (echo)	17.4 ± 2.7	15 ± 2
$g_{s,i}^{(2)\text{th}}$	13 ± 5	10 ± 3
$g_{s,i}^{(2)}$ (input)	12.6 ± 0.5	11.7 ± 0.4
r	$(2.1 \pm 0.4) \%$	$(3.4 \pm 0.5) \%$

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- [1] K. Hammerer, A. S. Sørensen, and E. S. Polzik, *Rev. Mod. Phys.* **82**, 1041 (2010).
- [2] H.-J. Briegel, W. Dür, J. I. Cirac, and P. Zoller, *Phys. Rev. Lett.* **81**, 5932 (1998).
- [3] N. Sangouard, C. Simon, H. de Riedmatten, and N. Gisin, *Rev. Mod. Phys.* **83**, 33 (2011).
- [4] H. P. Specht, C. Nölleke, A. Reiserer, M. Uphoff, E. Figueroa, S. Ritter, and G. Rempe, *Nature* **473**, 190 (2011).
- [5] T. Chanelière, D. N. Matsukevich, S. D. Jenkins, S.-Y. Lan, T. A. B. Kennedy, and A. Kuzmich, *Nature* **438**, 833 (2005).
- [6] C. W. Chou, H. de Riedmatten, D. Felinto, S. V. Polyakov, S. J. van Enk, and H. J. Kimble, *Nature* **438**, 828 (2005).
- [7] J. Simon, H. Tanji, J. K. Thompson, and V. Vuletic, *Phys. Rev. Lett.* **98**, 183601 (2007).
- [8] X. H. Bao, A. Reingrubern, P. Dietrich, J. Rui, A. Dück, T. Strassel, L. Li, N. L. Liu, B. Zhao, and J. W. Pan, *Nat. Phys.* **8**, 517 (2012).
- [9] A. G. Radnaev, Y. O. Dudin, R. Zhao, H. H. Jen, S. D. Jenkins, A. Kuzmich, and T. A. B. Kennedy, *Nat. Phys.* **6**, 894 (2010).
- [10] H. Zhang, X.-M. Jin, J. Yang, H.-N. Dai, S.-J. Yang, T.-M. Zhao, J. Rui, Y. He, X. Jiang, F. Yang, G.-S. Pan, Z.-S. Yuan, Y. Deng, Z.-B. Chen, X.-H. Bao, S. Chen, B. Zhao, and J.-W. Pan, *Nat. Photon.* **5**, 628 (2011).
- [11] B. Julsgaard, J. Sherson, J. I. Cirac, J. Fiurášek, and E. S. Polzik, *Nature* **432**, 482 (2004).
- [12] M. D. Eisaman, A. André, F. Massou, M. Fleischhauer, A. S. Zibrov, and M. D. Lukin, *Nature* **438**, 837 (2005).
- [13] K. F. Reim, P. Michelberger, K. C. Lee, J. Nunn, N. K. Langford, and I. A. Walmsley, *Phys. Rev. Lett.* **107**, 053603 (2011).
- [14] M. Hosseini, G. Campbell, B. M. Sparkes, P. K. Lam, and B. C. Buchler, *Nat. Phys.* **7**, 794 (2011).
- [15] W. Tittel, M. Afzelius, T. Chanelière, R. L. Cone, R. L. S. Kröll, S. A. Moiseev, and M. Sellars, *Laser Photon. Rev.* **4**, 244 (2010).
- [16] R. M. Macfarlane, *J. Lumin.* **100**, 1 (2002).
- [17] M. P. Hedges, J. J. Longdell, Y. Li, and M. J. Sellars, *Nature* **465**, 1052 (2010).
- [18] M. Sabooni, Q. Li, S. Kröll, L. Rippe, *Phys. Rev. Lett.* **110**, 133604 (2013).
- [19] H. de Riedmatten, M. Afzelius, M. U. Staudt, C. Simon, and N. Gisin, *Nature* **456**, 773 (2008).
- [20] M. Afzelius, C. Simon, H. de Riedmatten, and N. Gisin, *Phys. Rev. A* **79**, 052329 (2009).
- [21] I. Usmani, M. Afzelius, H. de Riedmatten, and N. Gisin, *Nature Comms.* **1**, 12 (2010).
- [22] M. Bonarota, J.-L. Le Gouët, and T. Chanelière, *New J. Phys.* **13**, 013013 (2011).
- [23] M. Gündoğan, M. Mazzera, P. M. Ledingham, M. Cristiani, and H. de Riedmatten, *New. J. Phys.* **15**, 045012 (2013).
- [24] M. Afzelius, I. Usmani, A. Amari, B. Lauritzen, A. Walther, C. Simon, N. Sangouard, J. Minář, H. de Riedmatten, N. Gisin, and S. Kröll, *Phys. Rev. Lett.* **104**, 040503 (2010).
- [25] N. Sinclair, E. Saglamyurek, H. Mallahzadeh, J. A. Slater, M. George, R. Ricken, M. P. Hedges, D. Oblak, C. Simon, W. Sohler, and W. Tittel, arXiv:1309.3202.
- [26] M. Sabooni, F. Beaudoin, A. Walther, N. Lin, A. Amari, M. Huang, and S. Kröll, *Phys. Rev. Lett.* **105**, 060501 (2010).
- [27] T. Chanelière, J. Ruggiero, M. Bonarota, M. Afzelius, and J.-L. Le Gouët, *New. J. Phys.* **12**, 023025 (2010).
- [28] M. Gündoğan, P. M. Ledingham, A. Almasi, M. Cristiani, and H. de Riedmatten, *Phys. Rev. Lett.* **108**, 190504 (2012).
- [29] Z.-Q. Zhou, W.-B. Lin, M. Yang, C.-F. Li, and G.-C. Guo, *Phys. Rev. Lett.* **108**, 190505 (2012).
- [30] N. Timoney, I. Usmani, P. Jobez, M. Afzelius, and N. Gisin, *Phys. Rev. A* **88**, 022324 (2013).
- [31] C. Clausen, I. Usmani, F. Bussièeres, N. Sangouard, M. Afzelius, H. de Riedmatten, and N. Gisin, *Nature* **469**, 508 (2011).
- [32] E. Saglamyurek, N. Sinclair, J. Jin, J. A. Slater, D. Oblak, F. Bussièeres, M. George, R. Ricken, W. Sohler, and W. Tittel, *Nature* **469**, 512 (2011).
- [33] I. Usmani, C. Clausen, F. Bussièeres, N. Sangouard, M. Afzelius, and N. Gisin, *Nature Photon.* **6**, 234 (2012).
- [34] C. Clausen, F. Bussièeres, M. Afzelius, and N. Gisin, *Phys. Rev. Lett.* **108**, 190503 (2012).
- [35] E. Saglamyurek, N. Sinclair, J. Jin, J. A. Slater, D. Oblak, F. Bussièeres, M. George, R. Ricken, W. Sohler, and W. Tittel, *Phys. Rev. Lett.* **108**, 083602 (2012).
- [36] G. Heinze, C. Hubrich, and T. Halfmann, *Phys. Rev. Lett.* **111**, 033601 (2013).
- [37] J. Fekete, D. Rieländer, M. Cristiani, and H. de Riedmatten, *Phys. Rev. Lett.* **110**, 220502 (2013).

- [38] Y. Sun, ‘*Rare Earth Materials in Optical Storage and Data Processing Applications*’ in G Liu and B Jacquier (Eds) ‘*Spectroscopic Properties of Rare Earths in Optical Materials*’. Berlin Heidelberg: Springer-Verlag, 2005.
- [39] M. Nilsson, L. Rippe, S. Kröll, R. Klieber, and D. Suter, Phys. Rev. B **70**, 214116 (2004).
- [40] M. Förtsch, J. Fürst, C. Wittmann, D. Strekalov, A. Aiello, M. V. Chekhova, C. Silberhorn, G. Leuchs, and C. Marquardt, Nature Comms. **4**, 1818 (2013).
- [41] F. Wolfram, Y. A. de Icaza Astiz, F. A. Beduini, A. Cerè, and M. W. Mitchell, Phys. Rev. Lett. **106**, 053602 (2011).
- [42] D. L. McAuslan, L. R. Taylor, and J. J. Longdell, Appl. Phys. Lett. **101**, 191112 (2012).
- [43] M. Bonarota, J. Ruggiero, J.-L. Le Gouët, and T. Chanelière, Phys. Rev. A **81**, 033803 (2010).
- [44] A. Kuzmich, W. P. Bowen, A. D. Boozer, A. Boca, C. W. Chou, L.-M. Duan, and H. J. Kimble, Nature **423**, 731 (2003).
- [45] P. R. Tapster and J. G. Rarity, J. Mod. Opt. **45**, 595 (1998).